

## MATH 103 - Final Exam Study Guide - Fall 2007

1:00–3:00 p.m. on Monday, December 10<sup>th</sup>

*Indicated page numbers refer to the appropriate section of the Course Notes.*

***Remember to bring a calculator with an exponential key ( $y^x$  or  $\wedge$ ) and a square root key.***

### Unit 1 - Growth Models

- Explain the difference between *linear* and *exponential* growth and their long-term behaviors. (pp. 2, 13, 18–21)
- Explain what is meant by “rate of change” (or “slope”) in a linear growth model. (pp. 3, 4 & 7)
- Write (and graph) an equation representing a population growing by either a *constant amount* each time period or a *constant percent* each time period. Use the equation to determine the size of the population at a given time. (pp. 3–6, 14, 17, 18 & 20)
- Explain the difference between *logistic* and *exponential* growth. (p. 22)

### Unit 2 - Probability (Material on “counting” is omitted from exam.)

- Compute an empirical probability based on experimental data. (pp. 2 & 4)
- Use a given probability to compute the number of times a particular outcome is expected to occur. (top of p. 8)
- Compute expected value of a random process. (pp. 26–30)
- What is the meaning of *expected value*? Should it be used to make conclusions about the short term (say, the next five observations) or the long run (many, many observations)? (pp. 27 & 28)
- What does the *Law of Large Numbers* say? (p. 2) How does it relate to tossing a fair die many, many times? What does it say about tossing a fair coin? (p. 28)

### Unit 3 - Working With Numerical Data

- Make histograms from given data and describe their shapes. (pp. 2–5)
- Compute the mean and median for a given set of data. How are they related to each other in a specific example? When is one more appropriate to use than the other? (pp. 6–11)
- Describe types of data that are well represented by a normal distribution. (pp. 13 & 14)
- Explain what the values  $\mu$  and  $\sigma$  tell you about a normal distribution. (p. 15)
- Know and use the “68-95-99.7 Rule” to describe a normal distribution. (p.16)
- Compute the margin of error for a survey and construct and interpret a *confidence interval* for a population percentage. (pp. 23–25)
- Describe the relationship between the margin of error and both the sample size and confidence level. (pp. 25–27)

### Unit 4 - Mathematics of Choice

- Analyze a set of possible alternatives (for example, investment options) using the five decision-making methods we discussed. (pp. 2–9)
- In a specific context, discuss which decision-making method might be appropriate. (p. 6)
- Describe the five voting methods and discuss their pros and cons. (pp. 10–13).
- Apply the five voting methods we discussed. (pp. 11–15)

**The following formulas will be the only ones provided on the exam:  $E.V. = \sum p_i x_i$      $m = z/2 \sqrt{n}$   
 You should know the appropriate formula for the other calculations listed on this sheet  
 (i.e., linear and exponential growth, mean, median, 68-95-99.7 Rule).**

You should review the following terms. You will be required **to match about half of these terms to their definitions.**

- |    |                                 |     |                                 |
|----|---------------------------------|-----|---------------------------------|
| a. | linear growth                   | aa. | sample                          |
| b. | exponential growth              | bb. | sampling bias                   |
| c. | slope (or rate of change)       | cc. | confidence interval             |
| d. | logistic growth                 | dd. | margin of error                 |
| e. | relative frequency              | ee. | confidence level                |
| f. | probability (i.e., theoretical) | ff. | compounding effect              |
| g. | empirical probability           | gg. | decision-making under certainty |
| h. | “fair” experiment               | hh. | criterion of pessimism          |
| i. | odds                            | ii. | criterion of optimism           |
| j. | expected value                  | jj. | criterion of equal probability  |
| k. | factorial                       | kk. | criterion of expected value     |
| l. | permutation                     | ll. | majority                        |
| m. | combination                     | mm. | plurality                       |
| n. | “Basic Counting Law”            | nn. | Condorcet method                |
| o. | frequency                       | oo. | Borda count                     |
| p. | histogram                       | pp. | approval voting                 |
| q. | median                          | qq. | undercoverage                   |
| r. | mean                            | rr. | nonresponse                     |
| s. | standard deviation              | ss. | response bias                   |
| t. | normal curve                    | tt. | voluntary response              |
| u. | z-value                         | uu. | leading question                |
| v. | symmetric                       |     |                                 |
| w. | skewed (right and left)         |     |                                 |
| x. | “68-95-99.7 Rule”               |     |                                 |
| y. | population                      |     |                                 |
| z. | sampling frame                  |     |                                 |